

(1001CJA102119078)

Test Pattern

**CLASSROOM CONTACT PROGRAMME**

(Academic Session : 2020 - 2021)

JEE(Advanced)
FULL SYLLABUS
20-05-2021
JEE(Main+ Advanced) : ENTHUSIAST COURSE [SCORE-II (PHASE-STAR BATCH)]**ANSWER KEY****PART-1 : PHYSICS**

	Q.	1	2	3	4	5	6	7	8	9	10
SECTION-I	A.	B,D	A,B,D	B,C,D	A,B,D	B,C,D	A,B	A,B	B	A	D
	Q.	11	12	13							
	A.	D	A	D							
SECTION-III	Q.	1	2	3	4	5					
	A.	5	2	9	5	2					

PART-2 : CHEMISTRY

	Q.	1	2	3	4	5	6	7	8	9	10
SECTION-I	A.	B,C	A,B,C,D	A,B,C,D	A,C,D	A,B,D	A,B,C	A,B,D	D	B	A
	Q.	11	12	13							
	A.	D	B	D							
SECTION-III	Q.	1	2	3	4	5					
	A.	5	4	0	8	7					

PART-3 : MATHEMATICS

	Q.	1	2	3	4	5	6	7	8	9	10
SECTION-I	A.	B,D	B,D	A,D	D	A,B,C,D	B,C,D	B,C	C	C	D
	Q.	11	12	13							
	A.	B	D	C							
SECTION-III	Q.	1	2	3	4	5					
	A.	7	6	5	4	2					

PART-1 : PHYSICS**SOLUTION****SECTION-I****1. Ans. (B,D)**

Sol. $r \propto \frac{1}{m}$

so m double, radius half

$E \propto m$

so IE will double and gap between levels will also double.

2. Ans. (A,B,D)**Sol.** When water is in liquid state

$$w_g = \frac{3}{2} mgh = k = \left[\frac{1}{2} mv^2 + \frac{1}{2} \left(\frac{2}{3} mr^2 \right) \frac{v^2}{r^2} \right] +$$

$$\left[\frac{1}{2} \left(\frac{m}{2} \right) v^2 \right]$$

water will have only translational KE when water is frozen

$$w_g = k' = \frac{3}{2} mgh = \frac{1}{2} mv'^2 + \frac{1}{2} \left(\frac{2}{3} mr^2 \right) \frac{v'^2}{r^2} +$$

$$\left[\frac{1}{2} \frac{m}{2} v'^2 + \frac{1}{2} \frac{2}{5} \frac{m}{2} r^2 \frac{v'^2}{r^2} \right]$$

water will have translational as well as rotational KE so $v' < v$ **3. Ans. (B, C, D)**

Sol. $\rho = kr^2 = \frac{\rho_0}{R^2} r^2$

(A) $v_{esc} = \sqrt{\frac{2GM}{R}}$

$$M = \int_0^R \frac{\rho_0}{R^2} r^2 4\pi r^2 dr = \frac{\rho_0 4\pi R^5}{R^2 \cdot 5} = \frac{\rho_0 4\pi R^3}{5}$$

$$\text{so } v_{esc} = \sqrt{\frac{2G\rho_0 4\pi R^3}{5R}} = \sqrt{\frac{8\pi G\rho_0 R^2}{5}}$$

(B) $g = \frac{GM}{r^2} = \frac{G}{r^2} \int_0^r \frac{\rho_0}{R^2} r^2 4\pi r^2 dr = \frac{G\rho_0 4\pi r^3}{5R^2}$

$$g \propto r^3$$

(C) as $v_{esc} = \sqrt{\frac{2GM}{R}}$ so will be same for other planet also.

(D) Energy required = $\frac{1}{2} mv_{esc}^2 \propto m$

$$\text{so } \frac{E_1}{E_2} = \frac{1}{2}$$

4. Ans. (A,B,D)

Sol. $V_A = \frac{Kq_A}{R} + \frac{Kq_B}{2R} = 2V,$

$$V_B = \frac{K(q_A + q_B)}{2R} = \frac{3}{2} V$$

$$\Rightarrow \frac{q_A}{q_B} = \frac{1}{2}$$

After earthing of B, $q'_A = q_A$ &

$$V'_B = \frac{K(q'_A + q'_B)}{2R} = 0$$

$$\Rightarrow \left| \frac{q'_A}{q'_B} \right| = 1 \quad \& \quad V'_A - V'_B = \frac{V}{2}$$

5. Ans. (B,C,D)

Sol. $|E| = \text{nat}^{n-1}$

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6. Ans. (A, B)

$$\text{Sol. } P = \frac{P_0}{2} \left[\sin \left(203\pi t + \frac{5\pi}{6} \right) + \sin \left(197\pi t + \frac{\pi}{6} \right) \right]$$

$$f_1 = \frac{203\pi}{2\pi} > 100$$

$$f_2 = \frac{197\pi}{2\pi} < 100$$

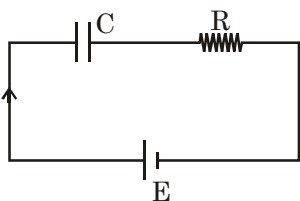
$$f_{\text{beat}} = \frac{203\pi}{2\pi} - \frac{197\pi}{2\pi} = 3$$

7. Ans. (A, B)

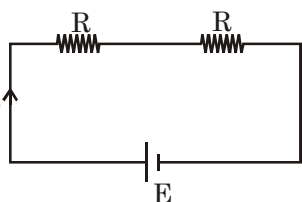
Sol. $\delta_{\text{net}} = \delta_1 + \delta_2 + \dots + \delta_n$
 where all have same magnitude and alternate deviations are in opposite direction.

8. Ans. (B)

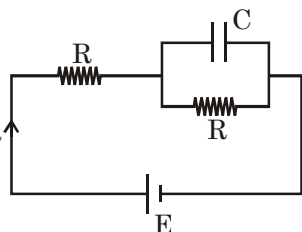
Sol. (I)



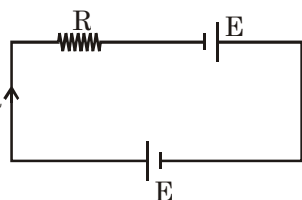
(II)



(III)



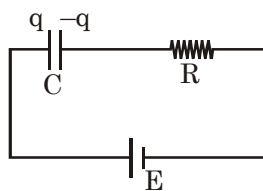
(IV)



Current in III & IV is maximum
 in (IV) no energy is stored as no capacitor
 so ans (B) IV, i, Q

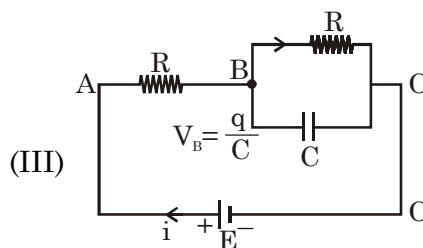
9. Ans. (A)

Sol. (I) At $t = RC$



$$q = CE(1 - e^{-1}) = \text{charge drawn from battery} = 0.63 CE$$

$$\text{(II) Charge drawn} = iRC = \frac{E}{2R} RC = 0.5CE$$



$$q = \frac{CE}{2} \left(1 - e^{-\frac{2t}{RC}} \right) \quad V_B = \frac{q}{C} \quad \& \quad V_A = E$$

$$i = \frac{V_A - V_B}{R} = \frac{E}{R} - \frac{E}{2R} \left(1 - e^{-\frac{2t}{RC}} \right)$$

$$= \frac{E}{2R} + \frac{E}{2R} e^{-\frac{2t}{RC}}$$

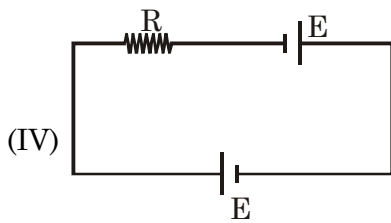
$$\text{Charge drawn} = \int_0^{RC} i dt = \frac{E}{2R} \int_0^{RC} \left(1 + e^{-\frac{2t}{RC}} \right) dt$$

$$= \frac{E}{2R} \left[\left(t + \frac{e^{-\frac{2t}{RC}}}{(-2)} (RC) \right) \right]_0^{RC}$$

$$= \frac{E}{2R} \left[\left(RC - \frac{RC}{2} e^{-2} \right) - \left(0 - \frac{RC}{2} \right) \right]$$

$$= \frac{E}{2R} \left[\frac{3RC}{2} - \frac{RC}{2} e^{-2} \right] = \frac{E}{2R} \frac{RC}{2} [3 - e^{-2}]$$

$$= \frac{CE}{4} (3 - e^{-2}) = 0.72 CE$$



charge drawn = $\frac{2E}{R}RC = 2CE$

10. Ans. (D)

Sol. in (III) $i_{t=0} = \frac{E}{R}$

$i_{t=\infty} = \frac{E}{2R}$

11. Ans. (D)

Sol. (I) F_{ABCD} due to $\rho_1 = \left(\rho_1 g \frac{h}{2}\right)h\ell$;

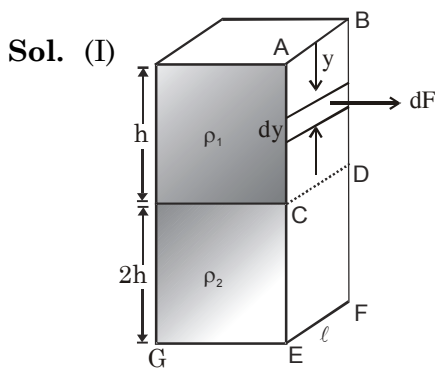
(II) F_{ABCD} due to $\rho_2 = 0$

(III) F_{CDEF} due to $\rho_1 = \rho_1 gh(2h\ell)$;

(IV) F_{CDEF} due to $\rho_2 = (\rho_2 gh)(2h\ell)$

Pressure at face CDEF due to ρ_1 is constant to effectively acts at centre

12. Ans. (A)

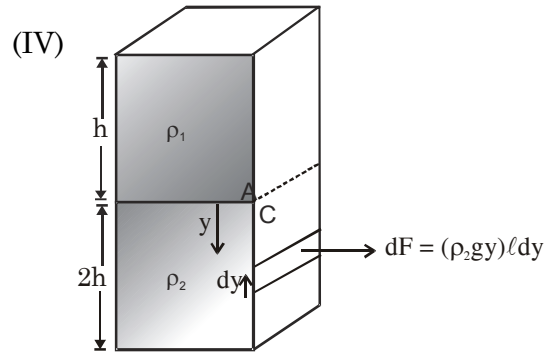


$\int d\tau = \int_0^h (\rho_1 gy) \ell dy (3h - y)$

$\tau = \rho_1 g \ell \left[\frac{3hy^2}{2} - \frac{y^3}{3} \right]_0^h = \rho_1 g \ell \frac{7}{6} h^3$

(II) $\tau = 0$

(III) $\tau = (\rho_1 gh)(2h\ell)(h) = 2\rho_1 gh^3\ell$



$\int d\tau = \int_0^{2h} (\rho_2 g \ell y dy)(2h - y)$

$\Rightarrow \tau = \rho_2 g \ell \left[2h \frac{y^2}{2} - \frac{y^3}{3} \right]_0^{2h}$

$= \rho_2 g \ell \left[h \cdot 4h^2 - \frac{8h^3}{3} \right] = \rho_2 g \ell \left[\frac{4h^3}{3} \right] = \frac{4\rho_2 g \ell h^3}{3}$

so $\frac{7}{6} \rho_1 g \ell h^3 < \frac{4}{3} \rho_2 g \ell h^3$ (as $\rho_1 = \rho_2$)

so minimum torque in (I)

13. Ans. (D)

Sol. Weight of liquid $\rho_2 = \rho_2(2h\ell)g = 2\rho_2\ell h^2g$

SECTION-III

1. Ans. 5

Sol. From COAM

$mv_0 \frac{\ell}{6} = \left(2m \left(\frac{\ell}{3} \right)^2 + m \left(\frac{2\ell}{3} \right)^2 \right) \omega$

$\omega = \frac{v_0}{4\ell}$

From COM

$mv_0 = 3mv_{cm}$

$v_{cm} = \frac{v_0}{3}$

Loss in KE

$= \frac{1}{2} mv_0^2 - \left\{ \frac{1}{2} (3m)v_{cm}^2 + \frac{1}{2} I_{cm}\omega^2 \right\}$

$= \frac{1}{2} mv_0^2 - \left\{ \frac{1}{2} (3m) \left(\frac{v_0}{3} \right)^2 + \frac{1}{2} \left(\frac{2m\ell^2}{3} \right) \left(\frac{v_0}{4\ell} \right)^2 \right\}$

$= \frac{15}{48} mv_0^2$

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2. Ans. 2

3. Ans. 9

Sol. Resistance of bulb, $R_{bulb} = \frac{V_{bulb}^2}{P_{bulb}} = 0.5\Omega$

In order to the bulb glows at full intensity, current will pass through the

$$I_{bulb} = \frac{4.5W}{1.5V} = 3A$$

equivalent resistance of circuit, R_{eq}

$$= \frac{5}{3} + \frac{0.5 \times 1}{0.5 + 1} = \frac{5}{3} + \frac{0.5}{1.5} = \frac{5}{3} + \frac{1}{3} = 2\Omega$$

$$\therefore \text{Current supplied by battery } \frac{E}{R_{eq}} = \frac{E}{2}$$

$$\text{Current in bulb} = I \times \frac{1}{(1+0.5)} \Rightarrow 3A =$$

$$\frac{I}{1.5} = \frac{E}{2 \times 1.5} \Rightarrow E = 9 \text{ volt.}$$

4. Ans. 5

Sol. Limiting friction between A & B = 90 N

Limiting friction between B & C = 80 N

Limiting friction between C & ground = 60 N

Since limiting friction is least between C and ground, slipping will occur at first between C and ground. This will occur when $F = 60 \text{ N}$.

5. Ans. 2

$$\text{Sol. } T = 2\pi\sqrt{\frac{I}{C}} \Rightarrow \frac{T'}{T} = \sqrt{\frac{I'}{I}} = \sqrt{\frac{\left(\pi \frac{4r^2}{2} t\right) 4r^2}{\frac{(\rho\pi r^2 t)r^2}{2}}}$$

$$T' = 2T$$

PART-2 : CHEMISTRY**SOLUTION****SECTION-I**

1. Ans.(B,C)

2. Ans.(A,B,C,D)

3. Ans.(A,B,C,D)

Sol. Borax on heating produces H_2O (neutral oxide) + $NaBO_2$ + B_2O_3 .

4. Ans.(A,C,D)

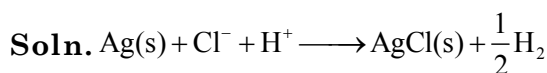
Sol. Decomposition reactions are endothermic in nature

$$\Delta_r S = \frac{\Delta_r H}{T} \text{ at equilibrium.}$$

$$\Delta_r G = \underbrace{\Delta_r H}_{+ve} - T \underbrace{\Delta_r S}_{-ve} \Rightarrow$$

(-ve) at high temperature.

5. Ans.(A,B,D)



$$E = 0 - (0.18) - 0.06 \log \frac{1}{[H^+][Cl^-]}$$

$$= -0.18 - 0.06 \times 6 = -0.54V$$

\therefore Cell will be represented as : $Pt | H_2 | HCl | AgCl | Ag$ & Cell potential = 0.54 V

$$E_{Cl^-|AgCl|Ag}^\circ = E_{Ag^+|Ag}^\circ + 0.06 \log K_{sp}(AgCl)$$

$$0.18 = E_{Ag^+|Ag}^\circ - 0.06 \times 10 \Rightarrow E_{Ag^+|Ag}^\circ = 0.78 \text{ volt}$$

6. Ans.(A,B,C)

7. Ans.(A,B,D)

8. Ans.(D)

0.1 M HCOOK

$$\Delta T_f = iK_f m \approx 2 \times 0.1 \times K_f = 0.2 K_f$$

$$\pi = 0.2RT$$

$$pOH = \frac{1}{2} [pK_w - pK_a - \log C] = \frac{1}{2} [14 - 4 + 1] = 5.5$$

$$pH = 8.5$$

Electrolysis products :

 CO_2, H_2 at anode: H_2 at cathode

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9. Ans.(B)

$$0.1 \text{ m Ca(NO}_3)_2$$

$$\Delta T_b = iK_b m = 0.3 K_b$$

$$\pi \approx 0.3RT$$

Electrolysis products : H_2 at cathode :
 O_2 at anode

$$\text{pH} = 7 \text{ (salt of S.A + S.B)}$$

10. Ans.(A)

0.1 M CH_3COONa + 0.2 M CH_3COOH
 \Rightarrow Acidic buffer solution

$$\pi = (i_1M_1 + i_2M_2)RT \approx (0.1 \times 2 + 0.2)RT$$

$$\approx 0.4RT$$

Electrolysis products : H_2 at cathode
: $\text{CO}_2, \text{C}_2\text{H}_6$ at
anode mainly

$$\text{pH} = \text{p}K_a + \log \frac{0.1}{0.2} = 5 - 0.3 = 4.7$$

11. Ans.(D)

12. Ans.(B)

13. Ans.(D)

SECTION-III

1. Ans.(5)

 Sol. $\text{B} = \text{CO}_2$

$$\text{D} = \text{C}_2\text{H}_2$$

2. Ans.(4)

(iii), (iv), (v), (vii)

3. Ans.(0)

 Sol. $x = 3$ (K, Rb, Cs)

$$y = 2$$
 (Mg, Be)

$u = 5$ (Concentrated solution of all alkali
 metals in liquid ammonia is blue
 coloured solution)

4. Ans.(8)

5. Ans.(7)

Solution: $\underset{(l\text{-form})}{\text{B}} \xrightleftharpoons[k_b]{k_f} \underset{(d\text{-form})}{\text{A}}$

$$t=0 \quad a \quad 0$$

$$t \quad a-x \quad x$$

$$t = t_{\text{eq}} \quad (a-x_{\text{eq}}) \quad x_{\text{eq}}$$

at equilibrium $\frac{dx}{dt} = k_f(a-x_{\text{eq}}) - k_b x_{\text{eq}} = 0$

$$\Rightarrow K_{\text{eq}} = \frac{k_f}{k_b} = \frac{x_{\text{eq}}}{a-x_{\text{eq}}}$$

Where, $x_{\text{eq}} = \frac{a}{2} \Rightarrow k_f = k_b$

$$(k_f + k_b) = \frac{2.303}{t} \log \left(\frac{x_{\text{eq}}}{x_{\text{eq}} - x} \right)$$

$$\Rightarrow 2k_f = \frac{2.303}{230.3} \log \frac{\frac{a}{2}}{\frac{a}{2} - \frac{a}{10}} = \frac{1}{100} \log \frac{0.5}{0.4}$$

$$= \frac{1}{100} (0.7 - 0.6) = 10^{-3} \text{ s}^{-1}$$

$$\therefore k_f = 5 \times 10^{-4} \text{ s}^{-1} = k_b$$

$$\therefore K_{\text{eq}} = 1 \Rightarrow \Delta_r G^\circ = 0, \Delta_r G = -ve$$

As A & B are enantiomers

$$\Rightarrow (S_m^\circ)_A = (S_m^\circ)_B$$

$$\text{and } \Delta_r H^\circ = 0, \Delta_r H = 0$$

PART-3 : MATHEMATICS

SOLUTION

SECTION-I

1. Ans. (B,D)

Sol. $\vec{a} \times \vec{b} = x\vec{a} + y\vec{b} + z\vec{c}$. Let $\vec{a} = \lambda\vec{b} \times \vec{c}$. $\lambda = \frac{1}{2}$

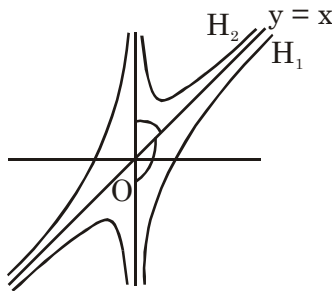
$$\begin{aligned} \text{So, } \frac{\vec{b} \times \vec{c}}{2} \times \vec{b} &= \frac{x}{2} \vec{b} \times \vec{c} + y\vec{b} + z\vec{c} \\ \Rightarrow -\frac{\vec{b}}{2} + \frac{\vec{c}}{6} &= \frac{x}{2} (\vec{b} \times \vec{c}) + y\vec{b} + z\vec{c} \\ \Rightarrow x &= 0, y = -\frac{1}{2}, z = \frac{1}{6} \end{aligned}$$

2. Ans. (B,D)

Sol. Integrating we get ; $x^2 + (f(x))^2 + (f'(x))^2 = k$
so, $f(x)$ and $f'(x)$ are bounded

3. Ans. (A,D)

Sol.



asymptote of $x^2 = xy + 1$ and $x^2 + 1 = xy$ are $x^2 - xy = 0$
and $y^2 - xy - 1 = 0$ and $x^2 - xy + 1 = 0$ are conjugate of each other

$$\Rightarrow \frac{1}{e_1^2} + \frac{1}{e_2^2} = 1 \text{ (direct result)}$$

for $x^2 + 1 = xy$ if we rotate the conic by $\frac{\pi}{8}$ it

$$\text{will be of the form } \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

with asymptotes $y = \pm \frac{b}{a}x \Rightarrow \frac{b}{a} = \tan \frac{\pi}{8}$

$$\Rightarrow e_2^2 = 1 + \frac{b^2}{a^2} = \frac{1}{1 + \cos \frac{\pi}{8}}$$

$$\Rightarrow \frac{1}{e_1^2} = 1 - \frac{1}{e_2^2} = 1 - \frac{1}{\sec \frac{\pi}{8}} = 1 - \cos \frac{\pi}{8}$$

$$\Rightarrow \left. \begin{aligned} e_1^2 &= \frac{1}{1 - \cos \frac{\pi}{8}} \\ e_2^2 &= \frac{1}{1 + \cos \frac{\pi}{8}} \end{aligned} \right\} \Rightarrow e_1 > e_2$$

4. Ans. (D)

$$\text{Sol. } p = \frac{2^{2 \times 2}}{2^{3 \times 3}} = \frac{1}{32}$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

Total number of matrices = 2^9

$(s_1 s_2 s_3 t_1 t_2 t_3)$ is odd integer if

(1) all the elements are 1 (no of matrices = 1)

(2) four zeros and five ones (no of matrices = 9)

(zeros must occupy all the positions of any minor)

(3) six zeroes and three ones

(no of matrices = 6)

$$({}^3C_1 \cdot {}^2C_1 \cdot 1)$$

$$\Rightarrow \text{required probability} = \frac{16}{2^9} = \frac{2^y}{2^9}$$

5. Ans. (A,B,C,D)

Sol. Given $AA^T = I$ and $|A| = 1$

$$\begin{aligned} \text{(A) } |A - I| &= |A - AA^T| = |I - A^T| \\ &= |(I - A^T)^T| \end{aligned}$$

$$|A - I| = |I - A| = -|A - I|$$

$$\Rightarrow |A - I| = 0$$

$$\text{(B) } |A^2 - I| = |A^2 - AA^T|$$

$$= |A| |A - A^T| = |A - A^T|$$

since $A - A^T$ is skew symmetric

$$\Rightarrow |A - A^T| = 0 \Rightarrow \text{hence is not invertible}$$

$$\text{(C) } |A - A^T| = 0 \Rightarrow (A - A^T)^2 \text{ is not invertible}$$

$$\text{(D) } (A - (\det A)) = A - I \text{ is not invertible}$$

6. **Ans. (B,C,D)**

Sol. Replace x by $-x$ we get ;

$$(2x^2 + 2x + 1)^n = \sum_{r=0}^{2n} a_r x^r$$

So, $\sum_{r=0}^{2n} a_r = 5^n, \sum_{r=0}^{2n} (-1)^r a_r = 1$. Also, $a_0 = 1$

again,

$$\sum_{r=0}^{2n} a_r x^r = ((x+1)^2 + x^2)^n = \sum_{k=0}^n {}^n C_k x^{2k} (x+1)^{2n-2k}$$

$$= \sum [{}^n C_k \sum {}^{2n-2k} C_t x^{2n-t}]$$

\Rightarrow comparing coeff. of x^{2n-r} , we get

$$\sum {}^n C_k {}^{2n-2k} C_r = a_{2n-r} = 2^{n-r} a_r$$

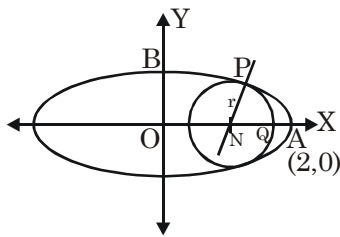
Also, $\sum_{r=0}^{2n} (-1)^r \cdot a_r a_{2n-r} = \text{coeff. of } x^{2n}$

in $((2x^2 - 2x + 1)^n (2x^2 + 2x + 1)^n)$

= coeff. of x^{2n} in $(4x^4 + 1)^n = 0$ if n odd.

7. **Ans. (B,C)**

Sol. $\frac{x^2}{4} + \frac{y^2}{3} = 1$



$N \equiv (k, 0)$ & $Q(r+k, 0)$
Normal PN at

$P(2 \cos \theta, \sqrt{3} \sin \theta)$; $\theta \neq \frac{n\pi}{2}$ is

$2x \sec \theta - \sqrt{3} y \csc \theta = 1$

$\Rightarrow N \equiv \left(\frac{\cos \theta}{2}, 0 \right) \Rightarrow k = \frac{\cos \theta}{2} \in \left(0, \frac{1}{2} \right)$

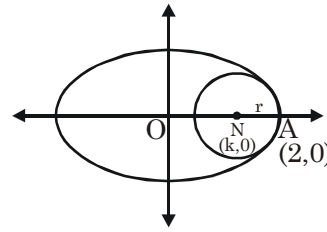
[as $k > 0$ & $\theta \neq \frac{n\pi}{2}$]

So, all such circles touches the arc of the ellipse in the 1st (as well as 4th) quadrant between (strictly) A & B.

Thus, $0 < k < \frac{1}{2}$ & $r+k < 2$ (as $Q_x < A_x$)

Now, these is another possibility when point of normalcy is A (note it cannot be B otherwise $k = 0$)

In this case,



$r+k = 2$

So, circle is

$(x-k)^2 + y^2 = (2-k)^2$

Intersecting it with given ellipse :

$3x^2 + 4[(2-k)^2 - (x-k)^2] = 12$

$\Rightarrow x^2 - 8kx + 16k - 4 = 0$

$\Rightarrow x = 2, 8k - 2$

Since, the circle lies completely inside the ellipse So, other point of intersection (i.e. $x = 8k - 2$) should be imaginary.

Hence, $8k - 2 > 2$ (Note $8k - 2 > -2$ as $k > 0$)

$\Rightarrow k > \frac{1}{2}$ & $r+k = 2$

(Matching Type)

Answer Q.8, Q.9 and Q.10

Sol. $x + y = 1$ represents a line

$x^2 + y^2 = 1$ represents a circle one of whose

tangents is $x + y = \sqrt{2}$ at point $\left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right)$

where as, $\sqrt{x} + \sqrt{y} = 1 \Rightarrow y = 1 + x - 2\sqrt{x}$

$\Rightarrow 4x = (1 + x - y)^2$ represents a parabola.

and $\frac{1}{x} + \frac{1}{y} = 1$ represents a hyperbola.

8. **Ans. (C)**

9. **Ans. (C)**

10. **Ans. (D)**

Answer Q.11, Q.12 and Q.13

Sol. (P) $[x] \{x\} = 1 \Rightarrow x \in \left\{ n + \frac{1}{n} : n \in \mathbb{I}, n \geq 2 \right\}$

(Q) $[x] \{x\} = 1 \Rightarrow x \in \left\{ n + \frac{1}{|n|} : n \in \mathbb{I}, |n| \geq 2 \right\}$

(R) $\left[x \left[\frac{1}{x} \right] \right] = 1 \Rightarrow x \in (-2, 0) \cup \left\{ \frac{1}{n} : n \in \mathbb{I}^+ \right\}$

(S) $\{x\} + \left\{ \frac{1}{x} \right\} = 1 \Rightarrow x \in \left\{ \frac{n \pm \sqrt{n^2 - 4}}{2} : n \in \mathbb{I}, |n| \geq 3 \right\}$

11. **Ans. (B)**

12. Ans. (D)

13. Ans. (C)

SECTION-III

1. Ans. 7

Sol. at $A = \frac{\pi}{7}, B = \frac{2\pi}{7}, C = \frac{4\pi}{7}$ which are angles of a triangle.

So, $x = \tan A, y = \tan B, z = -\tan C$.

$$\begin{aligned} & \frac{1}{2}(x^2 + y^2 + z^2 - x^2y^2z) \\ &= \frac{1}{2}[\tan^2 A + \tan^2 B + \tan^2 C - (\tan A \tan B \tan C)^2] \\ &= -(\tan A \tan B + \tan B \tan C + \tan C \tan A) \\ &= -\frac{\sin A \sin B \cos C + \sin B \sin C \cos A + \sin C \sin A \cos B}{\cos A \cos B \cos C} \\ &= \frac{\cos(A + B + C) - \cos A \cos B \cos C}{\cos A \cos B \cos C} \\ &= -\frac{1}{\cos \frac{\pi}{7} \cos \frac{2\pi}{7} \cos \frac{4\pi}{7}} - 1 = 8 - 1 = 7. \end{aligned}$$

2. Ans. 6

Sol. $f'(x) = 0 \Rightarrow x = -\frac{9}{5a}, \frac{1}{a}$

As, $a < 0$ and maxima comes first so,

$$\frac{1}{a} = -\frac{5}{9} \Rightarrow a = -\frac{9}{5} \text{ and } \alpha = 1$$

Now, $f(1) > 0 \Rightarrow b > \frac{36}{5} \Rightarrow a + b > \frac{27}{5}$

3. Ans. 5

Sol. Let $t = \frac{x^3 - 3x + 1}{x^2 - x} = \frac{(x^2 - x)(x + 1) - (x - 1) - x}{x^2 - x}$

$$= x + 1 - \frac{1}{x} - \frac{1}{x - 1}$$

So, $I = \int_{\frac{1}{12}}^{\frac{1}{6}} \frac{1}{t^2} dt = \left(-\frac{1}{t}\right) \Big|_{\frac{1}{12}}^{\frac{1}{6}} = 6 - \frac{12}{17} = \frac{90}{17}$

(for $x = -2, t = -\frac{1}{6}$ and for $x = -3,$

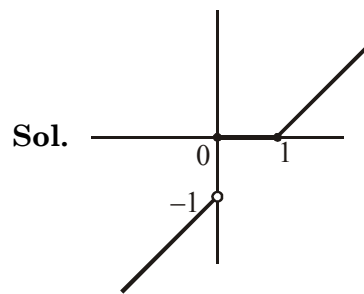
$$t = -\frac{17}{12})$$

4. Ans. 4

Sol. g is symmetrical about

$$x = \frac{\pi}{2}. \quad g_{\max} = g\left(\frac{\pi}{2}\right) = 2f\left(\frac{\pi}{2}\right) = 4$$

5. Ans. 2



Not differentiable at $x = 0, 1$